

Generative Models For Spatial-Based Bottom Hypoxia Forecasting In The Black Sea

Victor Mangeleer, Marilaure Grégoire and Gilles Louppe | University of Liège



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Can we **accurately forecast** ocean oxygen levels by assimilating **Earth observations** ?

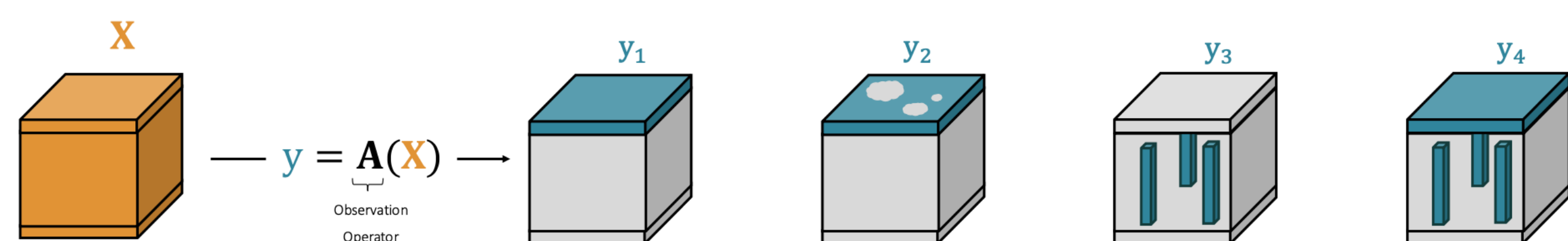
Problem Statement

The Black Sea can exist in different states $\mathbf{X}$, but **some are more probable than others**. When forecasting, we are interested in generating a **trajectory** of states $\mathbf{X}_{1:T}$:

$$P(\mathbf{X}_{1:T}) = P\left(\begin{array}{c} \text{Cube}_1 \\ 1 \end{array}, \begin{array}{c} \text{Cube}_2 \\ 2 \end{array}, \dots, \begin{array}{c} \text{Cube}_T \\ T \end{array}\right)$$

Mathematics 1: The notation $P(\mathbf{X}_{1:T})$ represents the distribution of all possible trajectories, or state evolutions, of the Black Sea. The orange cube indicates the state of the Black Sea at a specific timestep t . **Orange** highlights what we want to know.

An observation of the Black Sea, denoted as $\mathbf{y}$, provides partial information about $\mathbf{X}$:



Mathematics 2: Observations $\mathbf{y}$ vary widely. **Blue** indicates that the state has been observed and is known at this position, while grey indicates areas where the state is currently unknown.

Given an observation $\mathbf{y}$, can we estimate the **posterior distribution** $P(\mathbf{X}_{1:T} | \mathbf{y})$ of trajectories $\mathbf{X}_{1:T}$ for the Black Sea continental shelf bottom that align with observations $\mathbf{y}$:

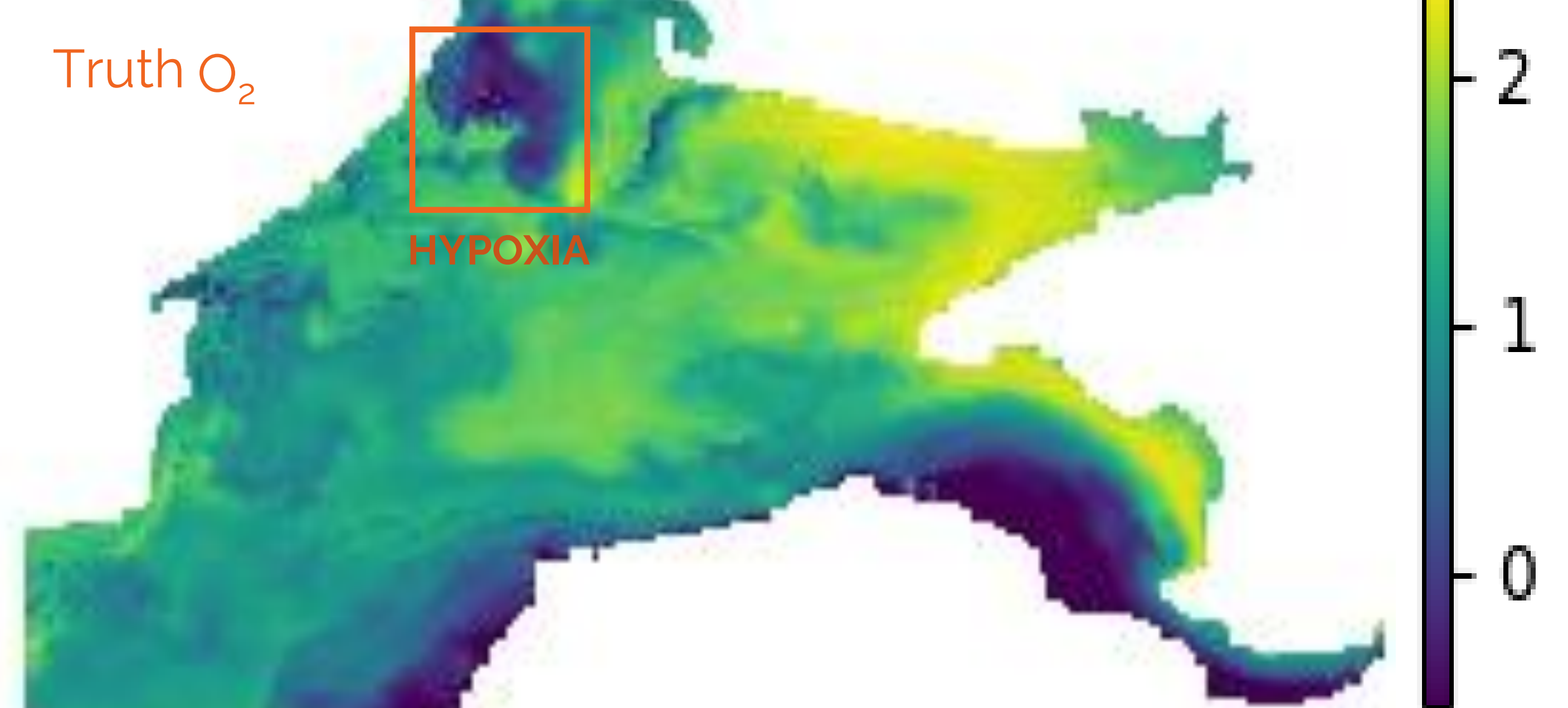
$$P(\mathbf{X}_{1:T} | \mathbf{y}) = P\left(\begin{array}{c} \text{Cube}_1 \\ 1:T \end{array} \mid \begin{array}{c} \text{Cube}_y \end{array}\right)$$

Mathematics 3: Accessing the posterior $P(\mathbf{X}_{1:T} | \mathbf{y})$ allows us to sample from this distribution, generating multiple forecasts for probabilistic trajectory forecasting.

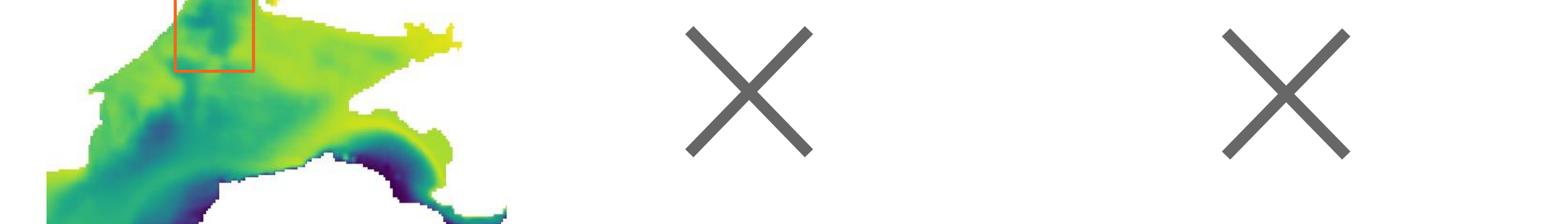
Results

Ground

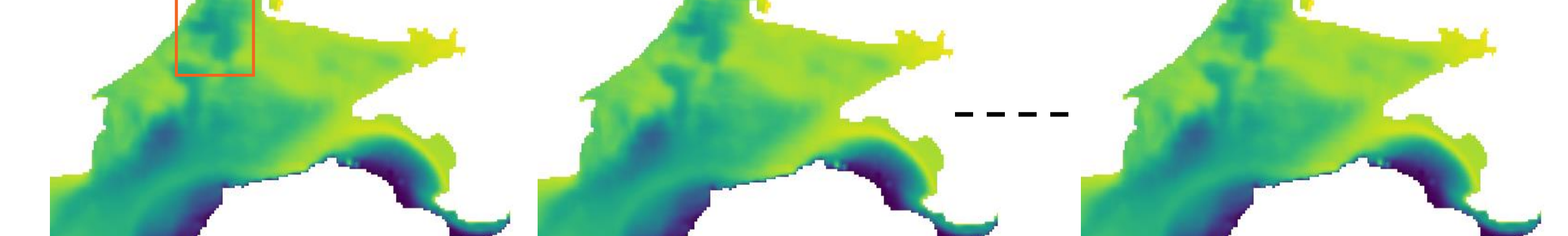
Truth O_2



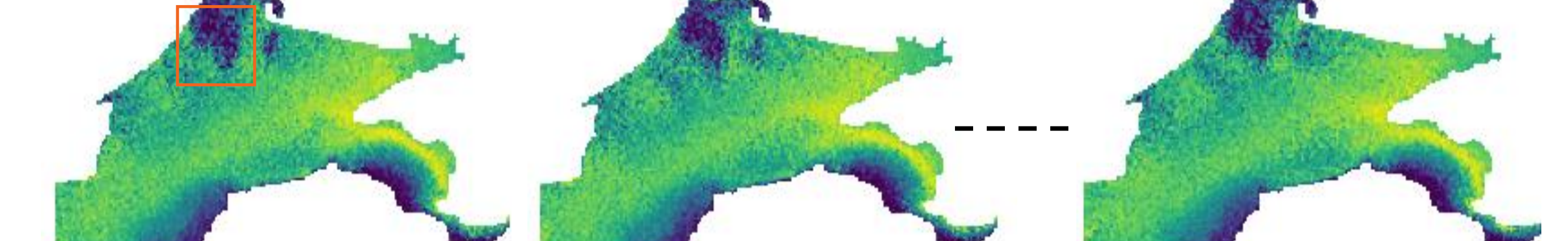
R



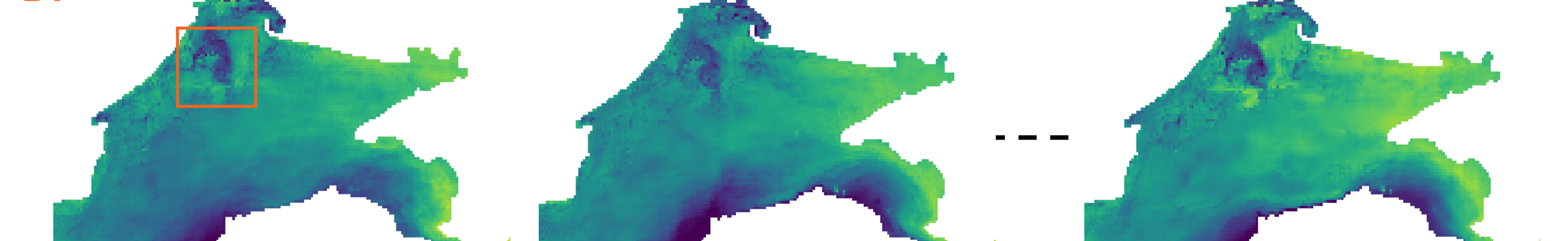
G



MoG



Di



$X_{t,1}$

$X_{t,2}$

$X_{t,3}$

Figure 2: At the top, we show the ground truth standardized oxygen profile at the bottom of the continental shelf X_1 on August 1st, 2016. A rare event, **hypoxia**, which typically occurs in summer, is highlighted in the red square. The rows represent different levels of posterior approximation, while each column shows a different oxygen state prediction $X_{t,1}, X_{t,2}, \dots$. They are obtained by sampling the posterior (if possible).

Posterior

The **posterior distribution** can be approximated by a **selected distribution** with parameters estimated by a Neural Network (with parameters θ), which is trained on Earth surface observations $\mathbf{y}$ from the present and/or past:

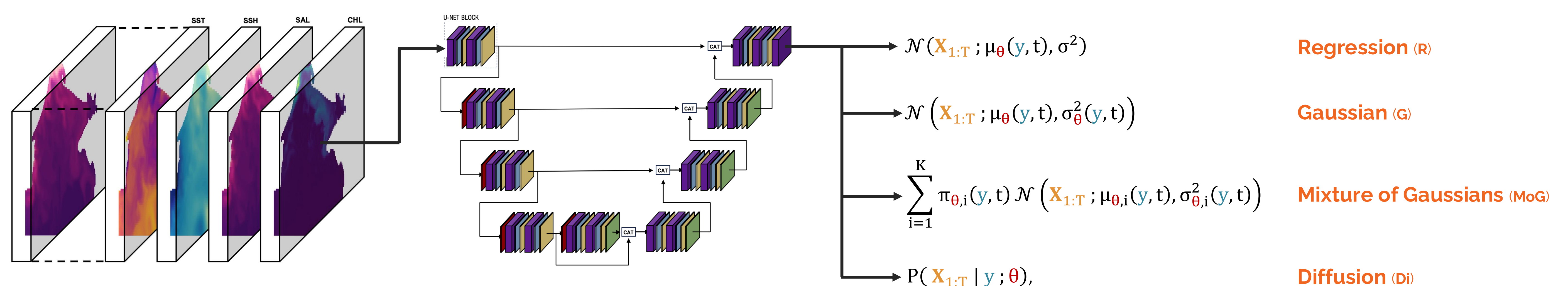


Figure 1: We observe temperature, salinity, chlorophyll, and sea surface height fields from the Black Sea surface. These observations can be from the current time t , the forecast moment, or a combination of past data. The observations $\mathbf{y}$ are then fed into a U-Net Neural Network, where each block is modulated by the forecast start date. Next, the **network predicts the parameters of the distribution** used to approximate our **posterior distribution** $P(\mathbf{X}_{1:T} | \mathbf{y})$. Finally, depending on the desired approximation level, we may sample trajectories from the posterior.